Guide to Factoring

How do I know which method to choose?

Always factor out any common factors first!

$$2x^2 + 8x - 10 = 0$$

$$2(x^2+4x-5)=0$$

$$2(x+5)(x-1)=0$$

$$x = -5$$
; $x = 1$

How many terms are there???

Common Perfect Squares:

$$1^2 = 1$$
 $7^2 = 49$

$$2^2 = 4$$
 $8^2 = 64$

$$3^2 = 9$$
 $9^2 = 81$

$$4^2 = 16$$
 $10^2 = 100$

$$5^2 = 25$$
 $11^2 = 121$

$$6^2 = 36$$
 $12^2 = 144$

2 Terms

Look for difference of 2 squares.

$$4x^2 - 9 = 0$$
$$(2x+3)(2x-3) = 0$$

$$x = -\frac{3}{2}$$
; $x = \frac{3}{2}$

Sum of 2 squares cannot be factored!!

$$4x^2 + 9 = 0$$

Cannot factor!

Leading coefficient = 1 Normal factoring!

$$x^{2} + 5x - 14 = 0$$
$$(x+7)(x-2) = 0$$
$$x = -7; x = 2$$

Leading coefficient ≠ 1 but not a perfect square trinomial? Slip and Slide!

3 Terms

Slip
$$3x^2 + 10x - 8 = 0$$

$$x^2 + 10x - 24 = 0$$
$$(x+12)(x-2) = 0$$

Slide
$$(x+\frac{12}{3})(x-\frac{2}{3})=0$$

$$(x+4)(3x-2) = 0$$

$$x = -4$$
; $x = \frac{2}{3}$

Perfect square trinomial?

When middle term is positive:

$$9x^2 + 12x + 4 = 0$$

$$(3x+2)(3x+2) = (3x+2)^2 = 0$$

$$(3x+2)=0$$

$$x = -\frac{2}{3}$$

When middle term is negative:

$$4x^2 - 10x + 25 = 0$$

$$(2x-5)(2x-5) = (2x-5)^2 = 0$$

$$(2x-5)=0$$

$$x = \frac{5}{2}$$