

Linear Inequalities & Systems of Inequalities

SHOW YOUR WORK!!

Define each of the following terms. Use your notes and the Carnegie Learning handout for chapter 7 if you need help.

- 1) Linear Inequality - the graph is a shaded region of the coordinate plane with a boundary line.
- 2) Systems of Linear Inequalities - two or more linear inequalities
- 3) Constraints - another name for inequalities in a system of linear inequalities because the solutions are "constrained" to the shaded region of the graph.

Fill in the blanks.

- 4) The ordered pairs are located in the shaded area of the graph and on the solid line.
- 5) Ordered pairs that make the inequality or inequalities true are called solutions.
- 6) Solutions for a system of inequalities are all the ordered pairs in the overlapping shaded region.
- 7) If the shaded regions do not overlap, there is no solution.

Determine if the graph of each linear inequality will have a DASHED or SOLID line AND if you shade ABOVE or BELOW the line.

8)  $y < 14x - 7$

dashed line  
 shade below

9)  $y - 9x \geq 3$

$\frac{+9x}{+9x} \frac{+9x}{+9x}$   
 $y \geq 9x + 3$   
 solid line  
 shade above

10)  $4x - 2y \leq 8$

$\frac{-4x}{-4x} \frac{-4x}{-4x}$   
 $\frac{-2y}{-2} \leq \frac{-4x}{-2} + \frac{8}{-2}$   
 $y \geq 2x - 4$   
 Flip the sign  
 solid line  
 shade above



11) Jacob can spend *no more than* \$4 for chips and candy. Chips cost \$1 each and candy costs \$0.50 each.

a. Write a linear inequality to represent the number of ways Jacob can spend \$4.

$x = \# \text{ of chips}, y = \# \text{ of candies}$

$$1x + 0.5y \leq 4$$

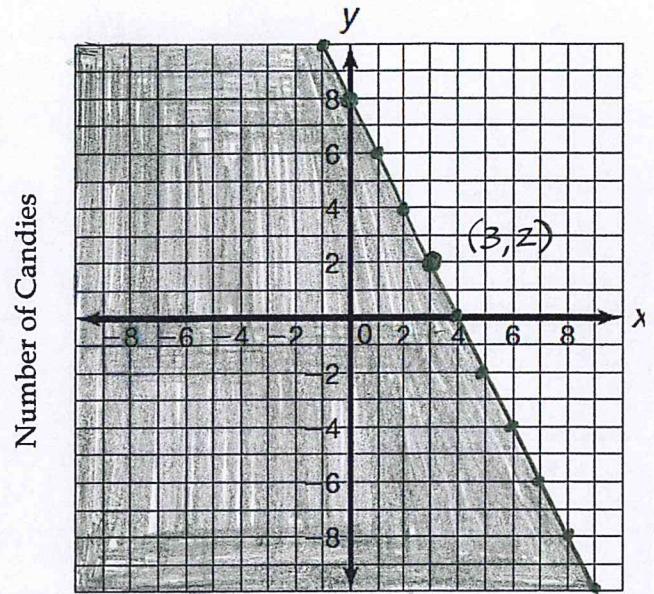
b. Graph the inequality. Don't forget to shade!

$$y \leq -2x + 8$$

*solid line, shade below*

c. Use the graph to determine if the ordered pair (3, 2) is a solution to the problem situation?

*Yes, (3, 2) is a solution.*



d. Prove algebraically that the ordered pair (4, 8) is a solution to the problem situation.

$$x=4, y=8 \quad 1(4) + 0.5(8) \leq 4$$

$$4 + 4 \leq 4$$

$8 \leq 4$  *No, (4, 8) is not a solution.*

e. Does the ordered pair (-2, -3) make sense as a solution in the context of this problem situation? Why or why not?

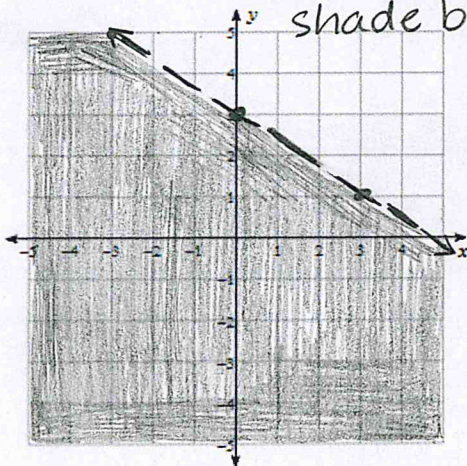
*No, you can't buy a negative number of chips or candy.*

Graph each of the linear inequalities.

12)  $y < -\frac{2}{3}x + 3$

$-\frac{2}{3}$  or  $\frac{2}{-3}$

*dashed line  
shade below*



13)  $x - 5y \geq -10$

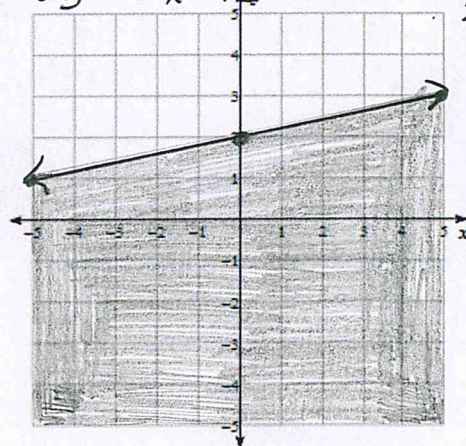
$$\frac{-x}{-5} \geq \frac{-x-10}{-5}$$

$$-5y \geq -x - 10$$

$$\frac{-5y}{-5} \geq \frac{-x}{-5} - \frac{10}{-5}$$

$$y \leq \frac{1}{5}x + 2$$

*solid line  
shade below*





Write a system of linear inequalities for each problem situation. Remember to define your variables.

- 14) Pablo's truck can carry a maximum of 1,000 pounds. He loads his truck with 20-pound bags of cement and 80-pound bags of cement. He plans to load at least 10 bags of cement into his truck.
- $x = \#$  20 lb bags of cement  
 $y = \#$  80 lb bags of cement
- $$\begin{cases} 20x + 80y \leq 1000 \\ x + y \geq 10 \end{cases}$$

- 15) Kathryn makes flower arrangements to sell in her shop. She can make a small arrangement in 30 minutes (or  $\frac{1}{2}$  hour) that sells for \$20. She can make a large arrangement in 1 hour that sells for \$50. Kathryn hopes to make at least \$350 by working no more than 8 hours.
- $x = \#$  of small arrangements  
 $y = \#$  of large arrangements
- $$\begin{cases} 20x + 50y \geq 350 \\ \frac{1}{2}x + 1y \leq 8 \end{cases}$$

Prove algebraically whether the given point is a solution to the system of linear inequalities.

16) 
$$\begin{cases} x + 5y < -1 \\ 2y \geq -3x - 2 \end{cases}$$

Point:  $(0, -1)$   $x=0, y=-1$

$$\begin{aligned} 0 + 5(-1) &< -1 & 2(-1) &\geq -3(0) - 2 \\ -5 &< -1 & -2 &\geq -2 \\ \text{yes/true} & & \text{yes/true} & \end{aligned}$$

$(0, -1)$  is a solution

17) 
$$\begin{cases} 4x + y < 21 \\ \frac{1}{2}x \leq 36 - 5y \end{cases}$$

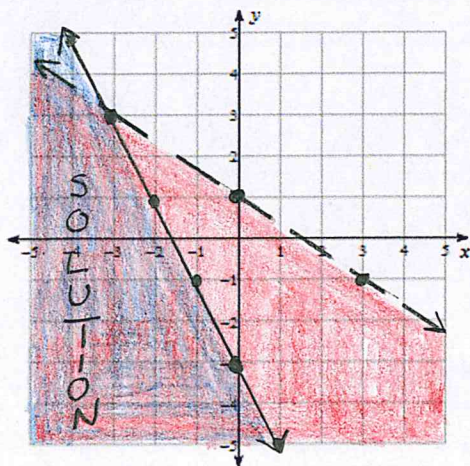
Point:  $(3, 7)$   $x=3, y=7$

$$\begin{aligned} 4(3) + 7 &< 21 & \frac{1}{2}(3) &\leq 36 - 5(7) \\ 19 &< 21 & 1.5 &\leq 36 - 35 \\ \text{yes/true} & & 1.5 &\leq 1 \\ & & \text{no/not true} & \end{aligned}$$

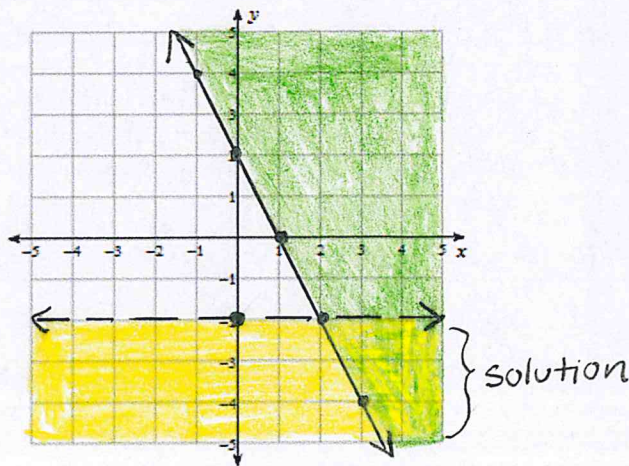
$(3, 7)$  is not a solution

Graph each system of linear inequalities.

18) 
$$\begin{cases} y \leq -2x - 3 \\ y < -\frac{2}{3}x + 1 \end{cases}$$

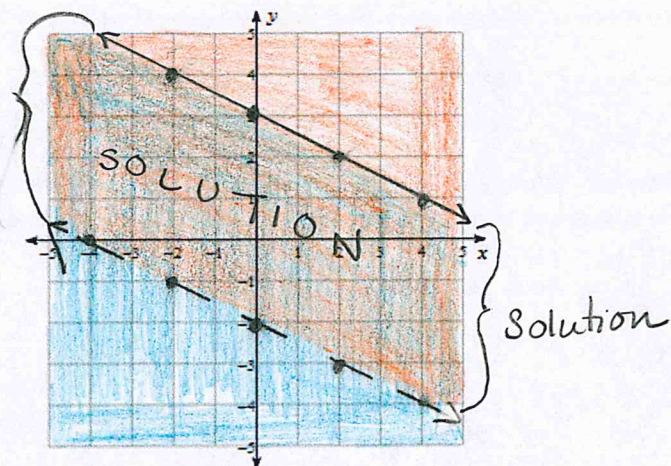


19) 
$$\begin{cases} y \geq -2x + 2 \\ y < -2 \end{cases}$$

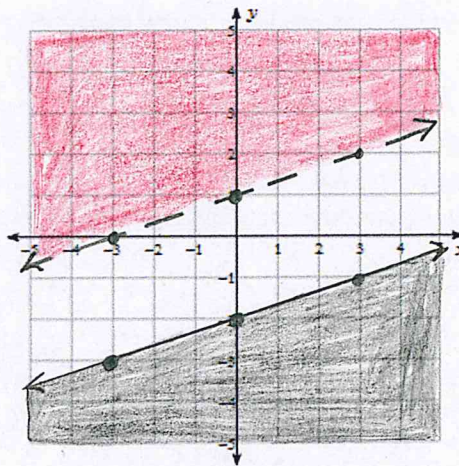




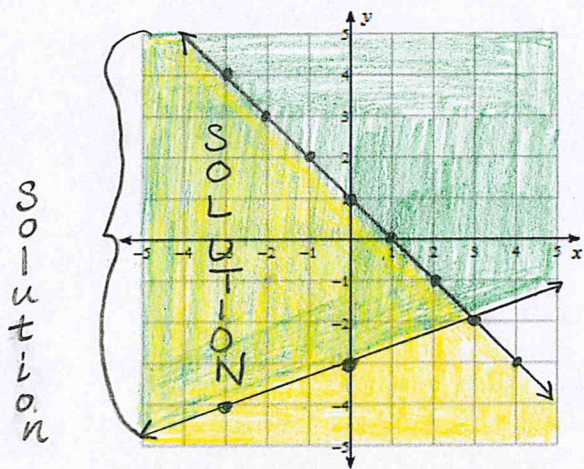
$$20) \begin{cases} y > -\frac{1}{2}x - 2 \\ y \leq -\frac{1}{2}x + 3 \end{cases}$$



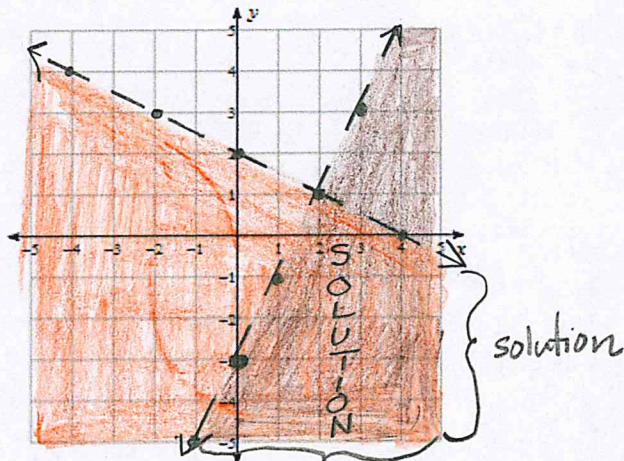
$$21) \begin{cases} y \leq \frac{1}{3}x - 2 \\ y > \frac{1}{3}x + 1 \end{cases}$$



$$22) \begin{cases} x + y \leq 1 & y \leq -x + 1 \\ x - 3y \leq 9 & y \geq \frac{1}{3}x - 3 \end{cases}$$



$$23) \begin{cases} x + 2y < 4 & y < -\frac{1}{2}x + 2 \\ 2x - y > 3 & y < 2x - 3 \end{cases}$$



$$\begin{array}{r} x + y \leq 1 \\ -x \quad -x \\ \hline y \leq -x + 1 \end{array}$$

$$\begin{array}{r} x - 3y \leq 9 \\ -x \quad -x \\ \hline -3y \leq -x + 9 \\ \frac{-3y}{-3} \leq \frac{-x + 9}{-3} \\ y \geq \frac{1}{3}x - 3 \end{array}$$

$$\begin{array}{r} x + 2y < 4 \\ -x \quad -x \\ \hline 2y < -x + 4 \\ \frac{2y}{2} < \frac{-x + 4}{2} \\ y < -\frac{1}{2}x + 2 \end{array}$$

$$\begin{array}{r} 2x - y > 3 \\ -2x \quad -2x \\ \hline -y > -2x + 3 \\ \frac{-y}{-1} > \frac{-2x + 3}{-1} \\ y < 2x - 3 \end{array}$$