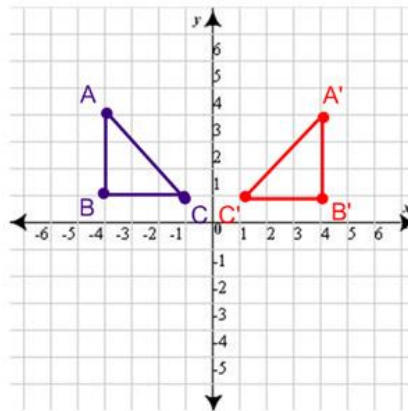


# Welcome Back!!



## Let's Begin the New Year by Reflecting Graphs



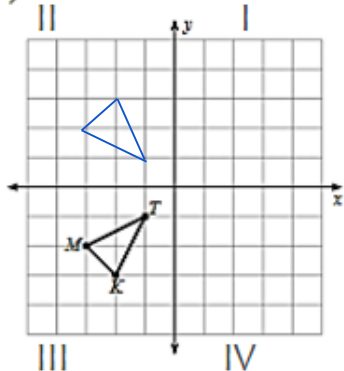
A. Identify the quadrant where each image will end up for the given reflection.

A. Which reflections are flipped up or down? These are **vertical** reflections.  
1 and 3

A. Which reflections are flipped left or right? These are **horizontal** reflections.  
2 and 4

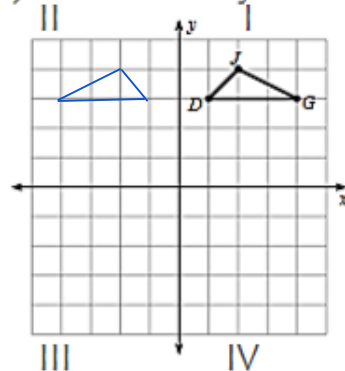
A. Do the  $x$ - or  $y$ -values change with a vertical reflection? Which values change with a horizontal reflection?  
Vertical Reflection:  $y$ -values change  
Horizontal Reflection:  $x$ -values change

1) reflection across the  $x$ -axis



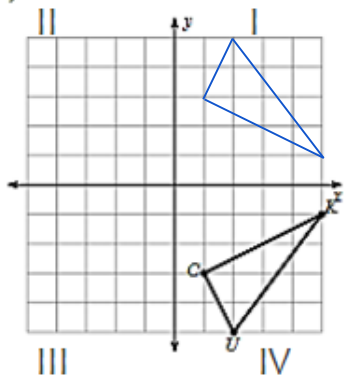
II

2) reflection across the  $y$ -axis



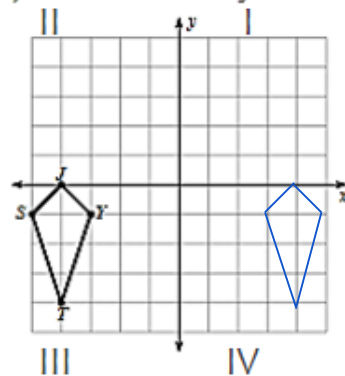
II

3) reflection across the  $x$ -axis



I

4) reflection across the  $y$ -axis



IV

Algebra 1: 5.4 Guided Notes  
Reflections of Linear and Exponential Functions

Name \_\_\_\_\_ Period \_\_\_\_\_



**Learning Goal**

- Reflect a function horizontally and vertically.

Notes

A reflection Flips a graph across a line of reflection (like the x or y axis)

The reflection is a mirror image of the original graph.

|          | <b>Horizontal Reflection</b>                   | <b>Vertical Reflection</b>                     |
|----------|--|--|
| Equation | $f(x) \rightarrow f(-x)$                       | <u><math>f(x) \rightarrow -f(x)</math></u>     |
| Table    | Only the x-values change signs (+/-)           | Only the y-values change signs (+/-)           |
| Graph    | Graph reflects/flips over the y-axis ( $x=0$ ) | Graph reflects/flips over the x-axis ( $y=0$ ) |

*Let's Practice!*

**Write the equation for the horizontal and vertical reflection of each function.**

1.  $f(x) = 5^x$

Horizontal reflection:  $5^{-x}$

Vertical reflection:  $-5^x$

2.  $f(x) = -2x^2$

Horizontal reflection:  $-2(-x)^2 = -2x^2$

Vertical reflection:  $-(-2x^2) = 2x^2$

3.  $f(x) = \frac{5}{4}x^3$

Horizontal reflection:  $\frac{5}{4}(-x)^3$

Vertical reflection:  $-\frac{5}{4}x^3$

## Let's Reflect an Exponential Function

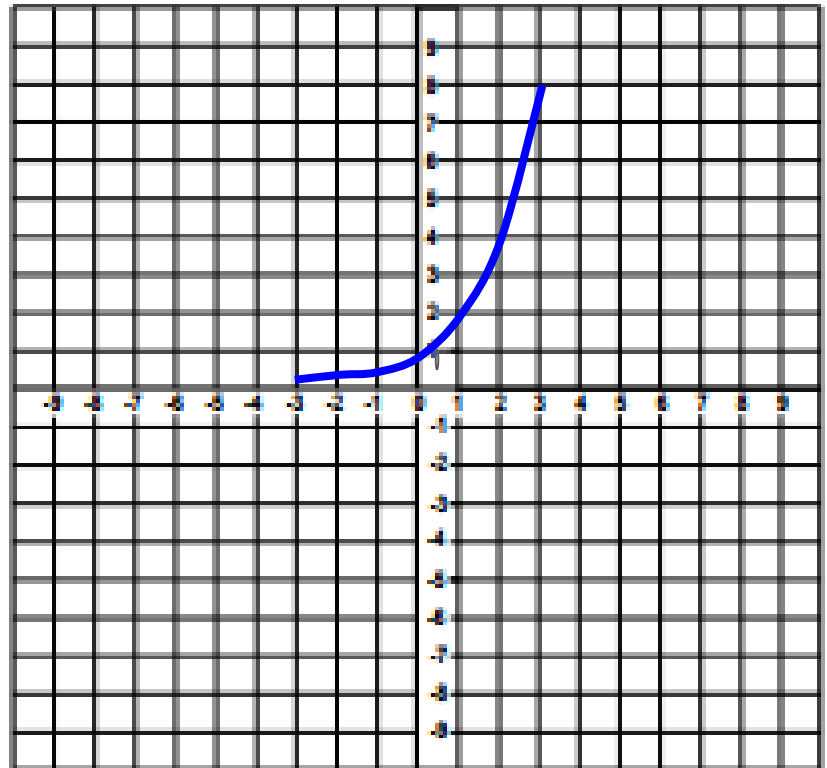
Equation

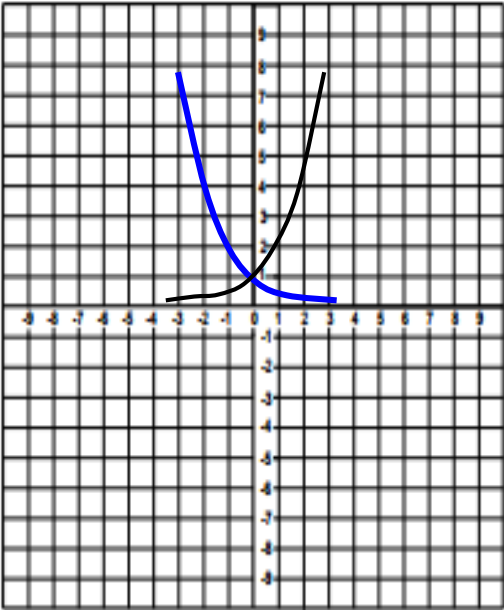
$$f(x) = 2^x$$

Table

| $x$ | $f(x) = 2^x$           |
|-----|------------------------|
| -3  | $2^{-3} = \frac{1}{8}$ |
| -1  | $2^{-1} = \frac{1}{2}$ |
| 0   | $2^0 = 1$              |
| 1   | $2^1 = 2$              |
| 3   | $2^3 = 8$              |

Graph

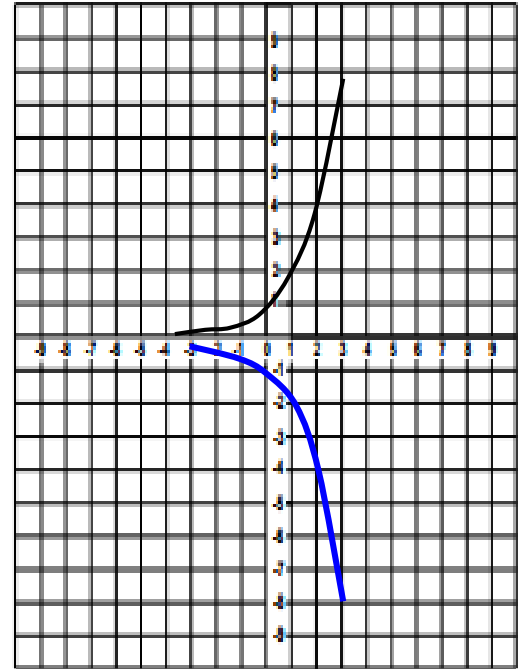


|                       | Equation                             | Table   | Graph |                             |   |               |   |               |   |   |    |   |    |   |   |
|-----------------------|--------------------------------------|---|-------|-----------------------------|---|---------------|---|---------------|---|---|----|---|----|---|---|
| Horizontal Reflection | $2^x \rightarrow \underline{2^{-x}}$ | <table border="1"> <thead> <tr> <th data-bbox="658 227 852 314"><math>x</math></th> <th data-bbox="852 227 1058 314"><math>f(x) = \underline{2^{-x}}</math></th> </tr> </thead> <tbody> <tr> <td data-bbox="658 314 852 407">3</td> <td data-bbox="852 314 1058 407"><math>\frac{1}{8}</math></td> </tr> <tr> <td data-bbox="658 407 852 494">1</td> <td data-bbox="852 407 1058 494"><math>\frac{1}{2}</math></td> </tr> <tr> <td data-bbox="658 494 852 582">0</td> <td data-bbox="852 494 1058 582">1</td> </tr> <tr> <td data-bbox="658 582 852 669">-1</td> <td data-bbox="852 582 1058 669">2</td> </tr> <tr> <td data-bbox="658 669 852 762">-3</td> <td data-bbox="852 669 1058 762">8</td> </tr> </tbody> </table> | $x$   | $f(x) = \underline{2^{-x}}$ | 3 | $\frac{1}{8}$ | 1 | $\frac{1}{2}$ | 0 | 1 | -1 | 2 | -3 | 8 |  |
| $x$                   | $f(x) = \underline{2^{-x}}$          |   |       |                             |   |               |   |               |   |   |    |   |    |   |   |
| 3                     | $\frac{1}{8}$                        |   |       |                             |   |               |   |               |   |   |    |   |    |   |   |
| 1                     | $\frac{1}{2}$                        |   |       |                             |   |               |   |               |   |   |    |   |    |   |   |
| 0                     | 1                                    |   |       |                             |   |               |   |               |   |   |    |   |    |   |   |
| -1                    | 2                                    |   |       |                             |   |               |   |               |   |   |    |   |    |   |   |
| -3                    | 8                                    |   |       |                             |   |               |   |               |   |   |    |   |    |   |   |

Vertical  
Reflection

$$2^x \rightarrow \underline{-2^x}$$

| $x$ | $f(x) = \underline{-2^x}$ |
|-----|---------------------------|
| -3  | $-\frac{1}{8}$            |
| -1  | $-\frac{1}{2}$            |
| 0   | -1                        |
| 1   | -2                        |
| 3   | -8                        |



# Homework: Worksheet