

Solving Quadratics by Factoring and Graphing

Factor each polynomial to determine the solution(s) or x -intercept(s), if possible. Then, graph the solution(s), the axis of symmetry, and the vertex.

$$1. \quad x^2 - 8x = -12 \quad \text{Move}$$

$$x^2 - 8x + 12 = 0$$

$$\begin{array}{r} -2 \cdot -6 = 12 \\ -2 + -6 = -8 \end{array}$$

$$(x-2)(x-6) = 0$$

$$x-2=0$$

$$\begin{array}{r} +2 \quad +2 \\ \hline x=2 \end{array}$$

$$x-6=0$$

$$\begin{array}{r} +6 \quad +6 \\ \hline x=6 \end{array}$$

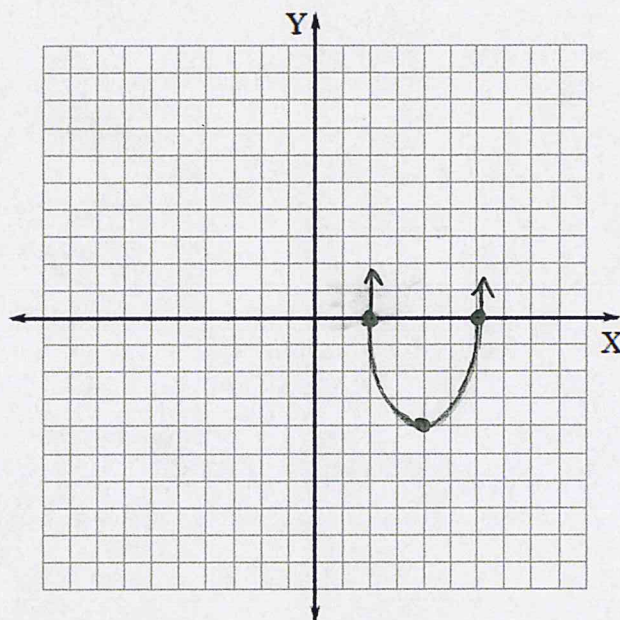
x -intercept(s): $(2,0)$ and $(6,0)$

axis of symmetry: $x = \frac{2+6}{2} = \frac{8}{2} = 4$

vertex: $(4, -4)$

$$x^2 - 8x + 12, \text{ Let } x=4$$

$$4^2 - 8(4) + 12 = 16 - 32 + 12 = -4$$



$$2. \quad x^2 = -9 - 6x \quad \text{Move}$$

$$x^2 + 6x + 9 = 0$$

$$\begin{array}{r} 3 \cdot 3 = 9 \\ 3 + 3 = 6 \end{array}$$

$$(x+3)(x+3) = 0$$

$$\text{or}$$

$$(x+3)^2 = 0$$

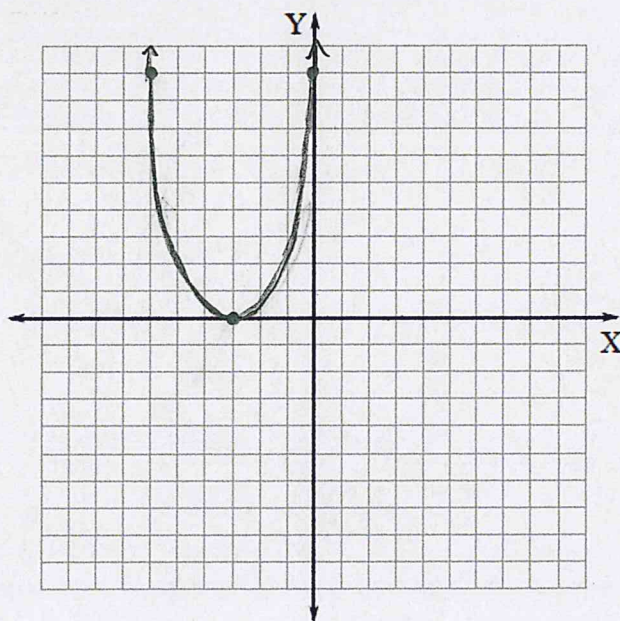
$$x+3=0$$

$$\begin{array}{r} -3 \quad -3 \\ \hline x=-3 \end{array}$$

x -intercept(s): $(-3,0)$

axis of symmetry: $x = -3$

vertex: $(-3,0)$



Parabola opens up

$$\pm 1x^2 + 6x + 9$$

↑ positive

$$3. \frac{2x^2-8}{2} = x^2-4$$

GCF \rightarrow $2(x^2-4)$

$$\frac{2 \cdot -2}{2} = -4$$

$$\frac{2 + -2}{2} = 0$$

$$2(x+2)(x-2) = 0$$

$$x-2=0$$

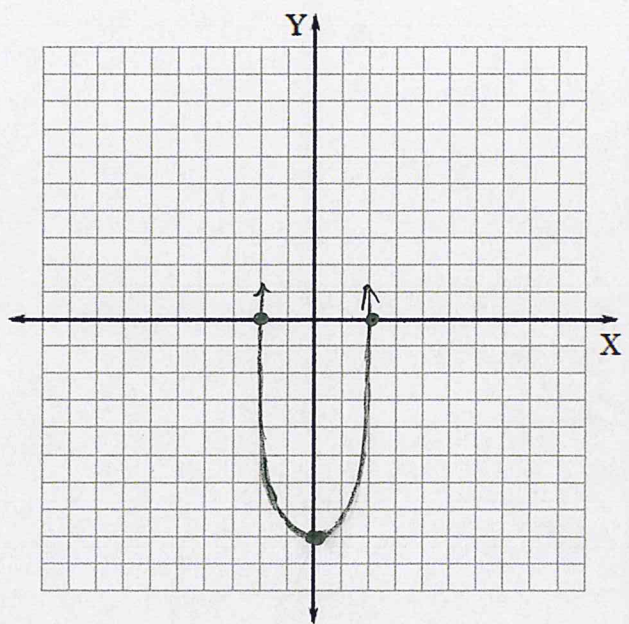
$$\frac{+2}{+2} = 2 \quad \boxed{x=2}$$

$$x+2=0$$

$$\frac{-2}{-2} = -2 \quad \boxed{x=-2}$$

x-intercept(s): $(2, 0)$ and $(-2, 0)$
 axis of symmetry: $x = \frac{2 + (-2)}{2} = \frac{0}{2} = 0$

vertex: $(0, -8)$
 $2x^2 - 8$, let $x=0$
 $2(0)^2 - 8 = 0 - 8 = -8$



$$4. \frac{-2x^2-12x-16}{-2} = x^2+6x+8$$

GCF \rightarrow $-2(x^2+6x+8)$

$$\frac{2 \cdot 4}{2} = 8$$

$$\frac{2 + 4}{2} = 6$$

$$-2(x+2)(x+4) = 0$$

$$x+2=0$$

$$\frac{-2}{-2} = -2 \quad \boxed{x=-2}$$

$$x+4=0$$

$$\frac{-4}{-4} = -4 \quad \boxed{x=-4}$$

x-intercept(s): $(-2, 0)$, $(-4, 0)$
 axis of symmetry: $x = \frac{-2 + (-4)}{2} = \frac{-6}{2} = -3$

vertex: $(-3, 2)$
 $-2x^2 - 12x - 16$, let $x = -3$
 $-2(-3)^2 - 12(-3) - 16$
 $-2(9) + 36 - 16$
 $-18 + 36 - 16$
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